



## Analysis of site effects in magnetotelluric data by using the multifractal detrended fluctuation analysis

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### ARTICLE INFO

#### Article history:

Received 6 September 2011

Received in revised form 22 March 2012

Accepted 5 April 2012

Available online 20 April 2012

#### Keywords:

Magnetotellurics

Detrended fluctuation analysis

### ABSTRACT

We investigated the multifractal structure of magnetic field  $H$  measured by magnetotelluric stations installed at three different sites in Taiwan, characterized by different site conditions. Magnetotelluric data include three components of the magnetic field  $H$ . We applied the multifractal detrended fluctuation analysis (MF-DFA) to magnetic magnitude time series (evaluated as the  $L^2$  norm). Our findings point out to a significant discrimination among these data in terms of multifractal characteristics of the signals, indicating a strong influence of the environmental settings of the measurement sites on the temporal fluctuations of magnetic field  $H$ . Such results highlight the usefulness of the MF-DFA in discriminating dynamics in observational time series of magnetotellurics.

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### 1. Introduction

Natural electromagnetic (EM) field in the Earth's sky is changed due to the solar wind and lightning activities and the secondary inductive EM wave is propagated in the solid Earth. The magnetotelluric (MT) method is a technique measuring the variation in the EM field on the Earth's surface for geological mapping of the subsurface structures (Chen and Chen, 1998; Chen et al., 2007). The MT data include two electric ( $E_x$ ,  $E_y$ ) and two magnetic ( $H_x$ ,  $H_y$ ) components, both in horizontal layouts with the north–south and east–west directions, and one vertical magnetic ( $H_z$ ) component. The fundamental MT transfer function between the amplitudes of electric and magnetic fields can be written as  $\mathbf{E}_i(\omega) = \mathbf{Z}_{ij}(\omega) * \mathbf{H}_j(\omega)$ , where  $\omega$  is the frequency and  $\mathbf{Z}$  is the impedance tensor related to the electrical properties of subsurface materials. Except for the conventional MT processing algorithms, recently, several tools of nonlinear time series analysis have been applied on MT data for extracting quantitative dynamical properties (Telesca et al., 2006; Balasco et al., 2007, 2008).

The potential of multifractal analysis is far from being fully exploited, since it was only rather recently that attention has been drawn to the need for a thorough testing of the multifractal tools, and, in particular, a much deeper understanding of the nature of the seismic phenomena and their interactions with the multifractal methods used for their analysis (Telesca et al., 2001, 2002, 2004b, 2005b; Telesca and Lapenna, 2006).

Recently analyzing the multifractal properties of geoelectrical signals measured in seismic areas, it was found a significant correlation between variation of multifractal degree and earthquakes. In particular it was found that geoelectrical signals measured in seismic areas are characterized by a larger multifractal degree than that of geoelectrical signals measured in areas with low seismicity (Telesca et al., 2003, 2004a). Significant increase of multifractal degree in geoelectrical signals was detected before the occurrence of relatively large seismic events (Telesca et al., 2004c, 2005a,c). Ultra Low Frequency (ULF) magnetic signals measured in Crete (Greece) revealed their multifractality and significant difference between horizontal and vertical components (Telesca et al., 2004d). Volcano-magnetic signals were investigated by MF-DFA, showing that the multifractal spectrum of pre-eruptive phase is wider than that of post-eruptive phase (Currenti et al., 2005). From these results it can be argued the potential of multifractal methods in revealing dynamical characteristics in geophysical time series.

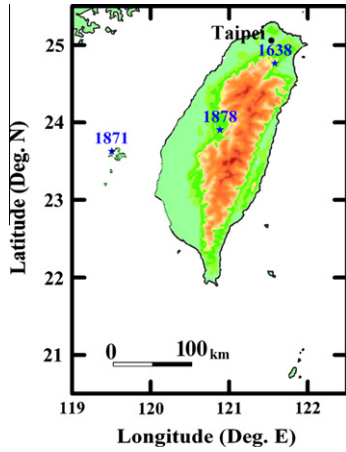
In this study, we analyzed the observed three magnetic channels of MT time series measured in Taiwan. In order to study the dynamics of these data, we used the multifractal detrended fluctuation analysis (MF-DFA). We clearly find that the multifractal behavior of the magnetic field is different in sites with different environmental conditions (e.g. oceanic- or landed-dominance).

### 2. Data description

The MT data analysed in this paper were continuously recorded with 15-Hz sampling rate by the MTU-5A systems (Phoenix Ltd., Canada) at three sites in Taiwan, indicated as 1871, 1878 and

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**Fig. 1.** Locations of MT observation sites (blue stars). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

1638 (Fig. 1). One site, 1871, is located in an area nearby the ocean, while the other two are located in areas relatively far from the ocean. The recording span is 1 week; the data were recorded at sites 1638 and 1878 from 5 September 2009 through 12 September 2009 and at site 1871 from 20 through 27 July 2009. We investigated the time dynamics of the 15-min averages of the three magnetic components at each site, for which the length scale of the penetration of the EM signal can approximate the crustal thickness. The possible difference between the three sites can also be due to the seasonal variation of the geomagnetic field (Yamazaki et al., 2011), but the long-period seasonal variation of geomagnetic field cannot be detected in our short-term records of 1 week.

### 3. Multifractal detrended fluctuation analysis

The main features of multifractals is to be characterized by high variability on a wide range of temporal or spatial scales, associated to intermittent fluctuations and long-range power-law correlations. The data examined in this paper present clear irregular dynamics (Fig. 2), characterized by fast fluctuations, which suggest to perform a multifractal analysis, in order to evidence different scaling behaviors for different intensities of fluctuations. We applied the multifractal detrended fluctuation analysis (MF-DFA), which operates on the series  $x(i)$ , where  $i = 1, 2, \dots, N$  and  $N$  is the length of the series (Kantelhardt et al., 2002). With  $x_{ave}$  we indicate the mean value. We assume that  $x(i)$  are increments of a random walk process around the average  $x_{ave}$ , thus the “trajectory” or “profile” is given by the integration of the signal

$$y(i) = \sum_{k=1}^i [x(k) - x_{ave}] \quad (1)$$

Next, the integrated series is divided into  $N_s = \text{int}(N/s)$  nonoverlapping segments of equal length  $s$ . Since the length  $N$  of the series is often not a multiple of the considered time scale  $s$ , a short part at the end of the profile  $y(i)$  may remain. In order not to disregard this part of the series, the same procedure is repeated starting from the opposite end. Thereby,  $2N_s$  segments are obtained altogether. Then we calculate the local polynomial trend for each of the  $2N_s$  segments by a least square fit of the series. Then we determine the variance

$$F^2(s, v) = \frac{1}{s} \sum_{i=1}^s \{y[(v-1)s + i] - y_v(i)\}^2 \quad (2)$$

for each segment  $v$ ,  $v = 1, \dots, N_s$  and

$$F^2(s, v) = \frac{1}{s} \sum_{i=1}^s \{y[N - (v - N_s)s + i] - y_v(i)\}^2 \quad (3)$$

for  $v = N_s + 1, \dots, 2N_s$ . Here,  $y_v(i)$  is the fitting line in segment  $v$ . Then, we average over all segments to obtain the  $q$ th order fluctuation function

$$F_q(s) = \left\{ \frac{1}{2N_s} \sum_{v=1}^{2N_s} [F^2(s, v)]^{\frac{q}{2}} \right\}^{\frac{2}{q}} \quad (4)$$

where in general, the index variable  $q$  can take any real value except zero. Repeating the procedure described above, for several time scales  $s$ ,  $F_q(s)$  will increase with increasing  $s$ . Then analyzing log–log plots  $F_q(s)$  versus  $s$  for each value of  $q$ , we determine the scaling behavior of the fluctuation functions. If the series  $x(i)$  is long-range power-law correlated,  $F_q(s)$  increases for large values of  $s$  as a power-law

$$F_q(s) \approx s^{h_q} \quad (5)$$

The value  $h_0$  corresponds to the limit  $h_q$  for  $q \rightarrow 0$ , and cannot be determined directly using the averaging procedure of Eq. (4) because of the diverging exponent. Instead, a logarithmic averaging procedure has to be employed,

$$F_0(s) \equiv \exp \left\{ \frac{1}{4N_s} \sum_{v=1}^{2N_s} \ln[F^2(s, v)] \right\} \approx s^{h_0} \quad (6)$$

In general the exponent  $h_q$  will depend on  $q$ . We call  $h_q$  the generalized Hurst exponent (Kantelhardt et al., 2002).  $h_q$  independent of  $q$  characterizes monofractal series. The different scaling of small and large fluctuations will yield a significant dependence of  $h_q$  on  $q$ . For positive  $q$ , the segments  $v$  with large variance (i.e. large deviation from the corresponding fit) will dominate the average  $F_q(s)$ . Therefore, if  $q$  is positive,  $h_q$  describes the scaling behavior of the segments with large fluctuations; and generally, large fluctuations are characterized by a smaller scaling exponent  $h_q$  for multifractal time series. For negative  $q$ , the segments  $v$  with small variance will dominate the average  $F_q(s)$ . Thus, for negative  $q$  values, the scaling exponent  $h_q$  describes the scaling behavior of segments with small fluctuations, usually characterized by larger scaling exponents.

From the generalized Hurst exponent, we can derive the multifractal spectrum. On the base of the relationship

$$\tau_q = qh_q - 1 \quad (7)$$

and then the Legendre transform (Parisi and Frisch, 1985),

$$\alpha = \frac{d\tau}{dq} \quad (8)$$

$$F_\alpha = q\alpha - \tau_q \quad (9)$$

where  $\alpha$  is the Hölder exponent and  $f_\alpha$  indicates the dimension of the subset of the series that is characterized by  $\alpha$  (Robertson et al., 2003).

### 4. Data analysis

We analysed the 1-week long 15-min averages of the magnitude of the magnetic field measured at three sites in Taiwan (labelled as station 1638, 1871 and 1878). The magnitude was calculated as the  $L^2$  norm:

$$H_t = \sqrt{H_{t,x}^2 + H_{t,y}^2 + H_{t,z}^2} \quad (10)$$

where the subscript  $t$  indicates the station and  $x$ ,  $y$  and  $z$  are the direction of the  $H$  component.

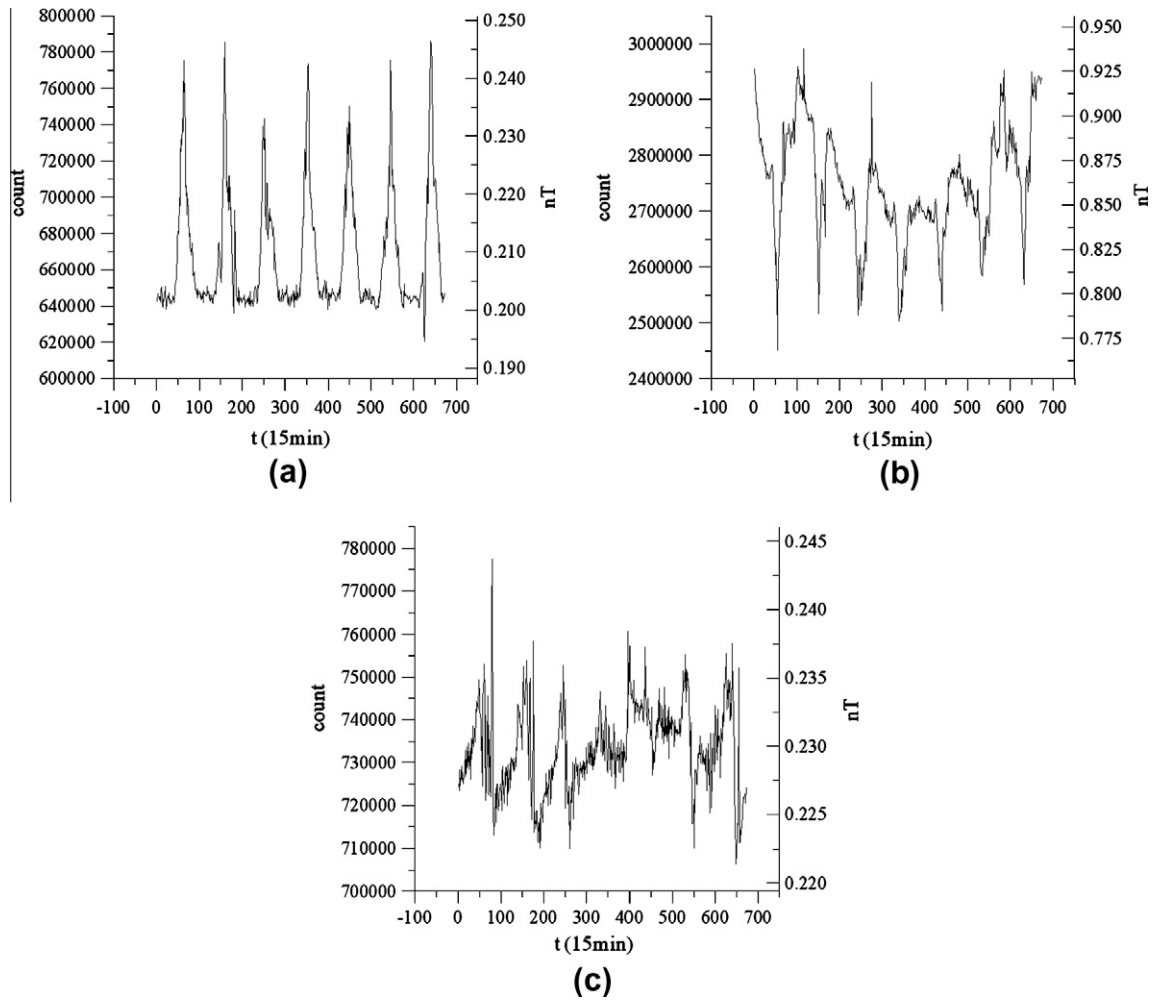


Fig. 2. Time variation of the  $H$  magnitude of the MT field at site 1871 (a), 1878 (b) and 1638 (c).

Fig. 2 shows the time variation of magnitude of the magnetic fields measured at the three stations. Most all the investigated variables have an oscillatory and spiky behavior, and this could affect the scaling behavior of the signals (Chen et al., 2002).

Let's examine the scaling behavior of  $H_{1871}$ . We applied the MF-DFA varying  $q$  from  $-5$  to  $+5$  and the scale  $s$  from 30 to  $N/4$ , being  $N$

the length of the series. Fig. 3 shows the fluctuation function  $F_5(s)$ , which is characterized by two scaling regimes separated by the crossover  $s_c \sim 95$  that is the period of the spiky wave superimposed to the signal  $H_{1871}$ . The generalized Hurst exponent in the first regime is  $h_5 \sim 0.95$ . Fig. 4 shows the fluctuation function  $F_{-5}(s)$ ; three different scaling regimes are clearly visible, separated by the

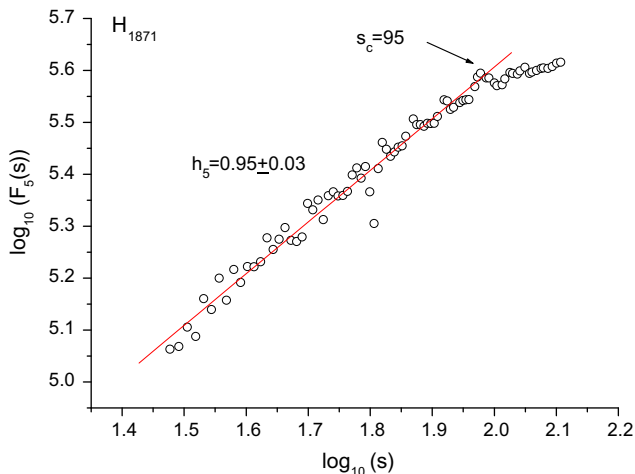


Fig. 3. Fluctuation function  $F_5(s)$  for  $H_{1871}$ .

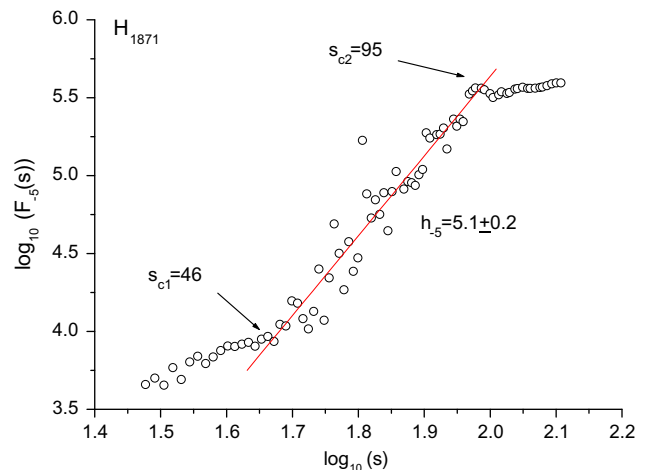


Fig. 4. Fluctuation function  $F_{-5}(s)$  for  $H_{1871}$ .

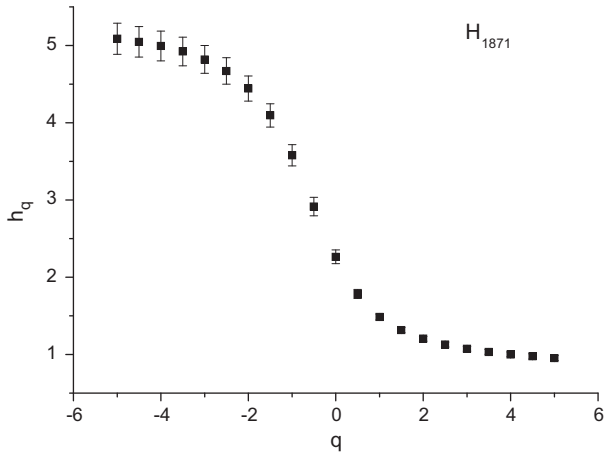


Fig. 5. Spectrum of generalized Hurst exponents for  $H_{1871}$ .

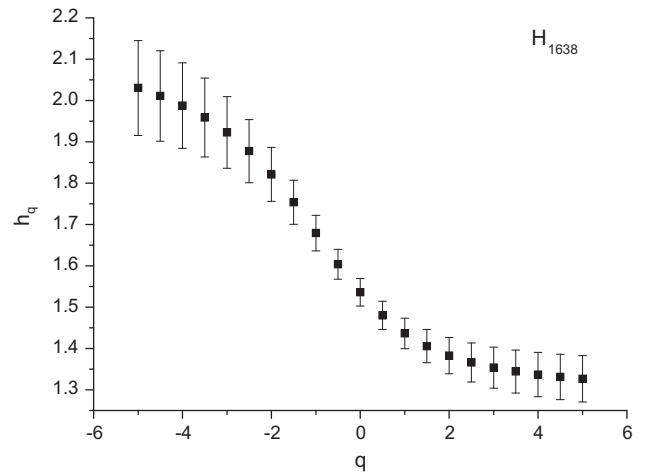


Fig. 8. Spectrum of generalized Hurst exponents for  $H_{1638}$ .

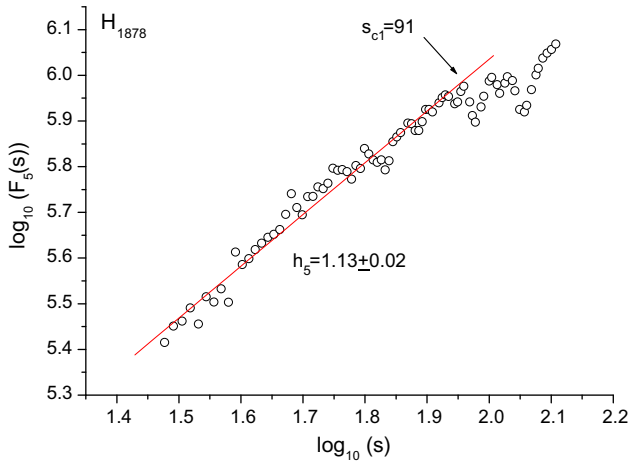


Fig. 6. Fluctuation function  $F_5(s)$  for  $H_{1878}$ .

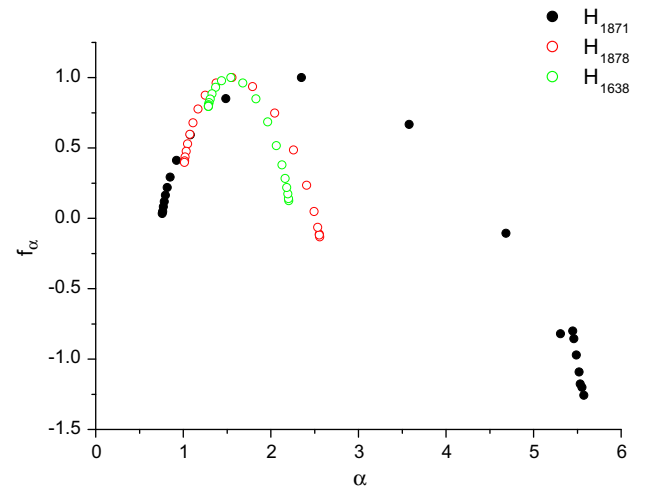


Fig. 9. Multifractal spectra.

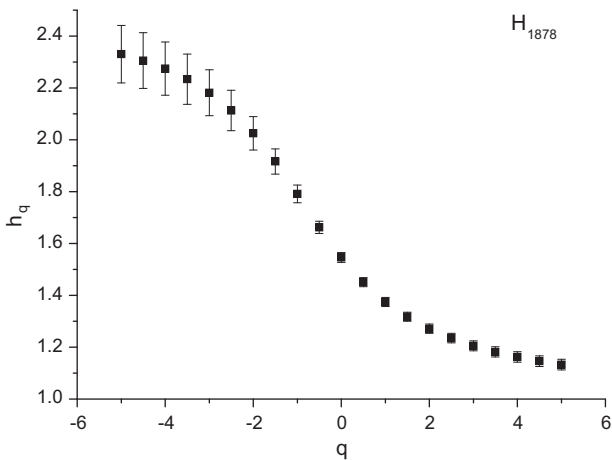


Fig. 7. Spectrum of generalized Hurst exponents for  $H_{1878}$ .

crossovers  $s_{c1} \sim 46$  and  $s_{c2} \sim 95$ . The crossover  $s_{c1}$  is consistent with the average width of the spikes in the signal  $H_{1871}$ . The scaling exponent  $h_{-5}$  is calculated within the range delimited by the two crossovers and is about 5.1. It is clear that the scaling depends on the oscillatory spiky behavior of the signal, and, therefore, the generalized Hurst exponents for any  $q$  were estimated in the

scaling range between the two crossovers  $s_{c1}$  and  $s_{c2}$ . The results are shown in Fig. 5. The spectrum of the generalized Hurst exponent  $h_q \sim q$  shows the typical multifractal behavior, with  $h_q$  monotonically decreasing with  $q$ .

Let's examine the multifractality of  $H_{1878}$ . Fig. 6 shows the fluctuation function  $F_5(s) \sim s$ . A crossover  $s_{c1} \sim 91$  is consistent with the period of the spikes and the generalized Hurst exponent  $h_5 \sim 1.13$ . The generalized Hurst spectrum  $h_q \sim q$  was, then, calculated for any  $q$  in the range  $s < s_{c1}$  (Fig. 7).

Following the same approach, the generalized Hurst spectra for  $H_{1638}$  was calculated for any  $q$  in the range  $s < s_{c1}$ , with  $s_{c1} = 67$  (Fig. 8).

Fig. 9 shows the multifractal spectra of the interevent times of the investigated seismicity and the quadratic fit. It is clearly evident that the width of the multifractal spectrum of  $H_{1871}$  is significantly larger than that of  $H_{1878}$  and  $H_{1638}$ .

In addition, we also applied conventional processing method of MT data and the resistivity-depth sections (Fig. 10) were computed at every sites by using the one-dimensional Occam inversion approach (Constable et al., 1987). The site 1871 contains a 1-km-thick layer with averagely  $10\text{-}\Omega\text{ m}$  in the shallow crust, which is very much different from the other two sites. Such low resistivity should be caused by the ocean effect to our MT data or the in situ crustal basalts.

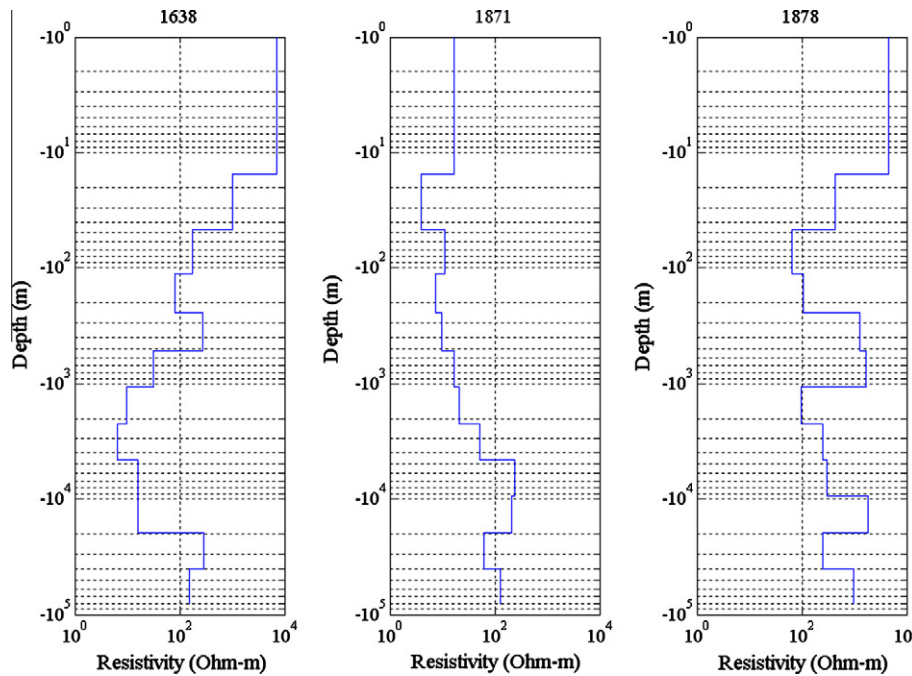


Fig. 10. 1D resistivity model of MT sites.

## 5. Discussion and conclusions

The results presented in this study show the multifractal nature of magnetic component of the MT filed measured in Taiwan. In particular, it has been shown that the degree of multifractality, which can be estimated by the width of the multifractal spectrum, is characterized by a visibly larger value for the magnetic signal measured in sites located in areas with relatively low seismic activity respect to the value of the width of the multifractal spectra of those magnetic signals recorded in areas with relatively very high seismic activity. The multifractality is an indication of the heterogeneity of the crust and could be presumably linked with the characteristic of the crustal seismogenic zones. The geology and environmental settings were much different between station 1871 and other sites on inland Taiwan (Angelier et al., 1990). Station 1871 is located at the basaltic area while the other two sites are located at the areas of sedimentary rocks with slight metamorphism. It is also however possible that the higher multifractal degree of the magnetic signal at station 1871 could be attributed to the hybrid effects of crustal and oceanic electrical circumstances. It is well-known to the MT community that parts of the long-period magnetic energies are generated from electrical currents carried by the oceanic brine currents (Chen and Chen, 1998; Chiang et al., 2010). Strong tidal effects in geoelectric potential field have been also found at the Nijima, Japan station (Huang and Liu, 2006). The lower resistivity at station 1871 (Fig. 10) may induce the stronger magnetic signal changed with the variation of magnetic filed. The signal  $H_{1871}$  may be thus included the stronger response of the EM induced from the ocean and igneous rocks.

Even if firm conclusions about the multifractal discrimination between MT magnetic signals measured in different geological settings should be further verified by using longer data sets recorded in more sites with different tectonic settings, it is, however, striking how the MF-DFA method is capable to extract quantitative information about the dynamics of such signals, which are obviously very complex. In any case, it is clearly evident that the multifractality is a feature for discriminating magnetic MT signals due to the site effects.

## Acknowledgements

This study was supported by the Bilateral Project CNR-NSC 2012–2013 “Advanced time series analysis tools for magnetotelluric data”. CCC acknowledges the NSC Grant 101-2923-M-008-003-MY2.

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